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Rachel Domagalski* (domag1rj@cmich.edu), **Hong Suh** and **Xingyu Zhang**. *Tight Frame Structure and Scalability*. Preliminary report.

In \mathbb{R}^n , a frame is defined to be a spanning set. A collection $F = \{f_i\}_{i=1}^k \subseteq \mathbb{R}^n$ is a λ -tight frame if there exists $\lambda > 0$ such that for every $f \in \mathbb{R}^n$, $\lambda\|f\|^2 = \sum_{i=1}^k |\langle f, f_i \rangle|^2$. We examine the structure of frames through factor posets and scalability. A factor poset for a frame $F = \{f_i\}_{i=1}^k$ is the set $P = \{J \subseteq \{1, \dots, k\} : \{f_j\}_{j \in J} \text{ is a tight frame}\}$, partially ordered by set inclusion, $\emptyset \in P$. This definition leads to the question: given a poset P , when is P a factor poset? We call this problem the *inverse factor poset problem* (IFPP). The IFPP was solved in \mathbb{R}^2 in 2013. In our goal of solving the IFPP in \mathbb{R}^n , we discovered combinatorial properties of tight frames and explored constructions of frames from posets. Next, we examine the scalability of frames. For a frame $F = \{f_i\}_{i=1}^k$, a scaling is a vector $w = (w(1), \dots, w(k)) \in \mathbb{R}_{\geq 0}^k$ such that $\{\sqrt{w(i)}f_i\}_{i=1}^k$ is a 1-tight frame in \mathbb{R}^n . We establish results on the structure of the scalability polytope and its connection to the factor poset. This research completed at Central Michigan University's 2014 REU. (Received September 04, 2014)