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**Alexander (Oleksandr) V Tovstolis\*** (atovstolis@math.okstate.edu), Oklahoma State University, Department of Mathematics, 401 Mathematical Sciences, Stillwater, OK 74078. *On the Mahler Measure of the Hadamard Product of Polynomials.*

The Hadamard Product of two polynomials  $P(z) = \sum_{k=0}^n p_k z^k$  and  $Q(z) = \sum_{k=0}^n q_k z^k$  is given by  $(P * Q)(z) = \sum_{k=0}^n p_k q_k z^k$ .

For Hardy spaces  $H^p$  ( $0 < p \leq \infty$ ) and the space of Mahler measure,  $H^0$ , in the unit disk  $\mathbb{D}$  of the complex plane, we obtained the following estimate:

$$(1) \quad \|P * Q\|_{H^p} \leq \|\Theta_n\|_{H^0} \|P\|_{H^0} \|Q\|_{H^p}, \quad 0 \leq p \leq \infty,$$

where

$$\Theta_n(z) := \sum_{k=0}^n \binom{n}{k}^2 z^k.$$

For  $p = 0$ , equality in (1) is achievable, e.g., taking  $P(z) = Q(z) = (1 + z)^n$ .

Furthermore,

$$\lim_{n \rightarrow \infty} \|\Theta_n\|_{H^0}^{1/n} = \exp\left(\frac{4G}{\pi}\right) \approx 3.20991230072 \dots,$$

where  $G = \sum_{m=0}^{\infty} \frac{(-1)^m}{(2m+1)^2}$  is Catalan's constant.

As an illustration of the method, estimates for the Mahler measure and the  $H^p$ -pre-norm of the odd and even parts of a polynomial were derived. (Received September 10, 2014)