1106-33-100 Xiaolong Han* (xiaolong.han@anu.edu.au), Department of Mathematics, Australian National University, Canberra, ACT 0200, Australia. Spherical harmonics with maximal norm growth.
Sogge's Lp estimates bound the Lp norms of normalized eigenfunctions on smooth and compact manifolds. They are also sharp on the sphere, with maximizers as Gaussian beams for small p and zonal harmonics for large p. In this talk, we investigate the density of these maximizers in the orthonormal eigenfunction basis, and construct a positive density subsequence of orthonormal spherical harmonics which achieves the maximal Lp norm growth for all small p. This gives an example of a Riemannian surface supporting such subsequence of eigenfunctions. Furthermore, we provide an explicit lower bound on the density in this example. (Received July 16, 2014)