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Differentiation with Respect to Parameters of Solutions of Nonlocal Boundary Value Problems for Difference Equations.

For the n th order difference equation, $\Delta^n u = f(t, u, \Delta u, \dots, \Delta^{n-1} u, \lambda)$, the solution of the boundary value problem satisfying $\Delta^{i-1} u(t_0) = A_i, 1 \leq i \leq n-1$, and $u(t_1) - \sum_{j=1}^m a_j u(\tau_j) = A_n$, where $t_0, \tau_1, \dots, \tau_m, t_1 \in \mathbb{Z}, t_0 < \dots < t_0 + n - 1 < \tau_1 < \dots < \tau_m < t_1$, and $a_1, \dots, a_m, A_1, \dots, A_n \in \mathbb{R}$, is differentiated with respect to the parameter λ . This talk will discuss the new theorem we proved that $\frac{\partial u}{\partial \lambda}$ exists on $[t_0, +\infty)_{\mathbb{Z}}$, and $w(t) := \frac{\partial u}{\partial \lambda}(t)$ is the solution of the nonhomogeneous linear equation, $\Delta^n z = \sum_{i=1}^n \frac{\partial f}{\partial s_i}(t, u(t), \dots, \Delta^{n-1} u(t), \lambda) \Delta^{i-1} z + \frac{\partial f}{\partial \lambda}(t, u(t), \dots, \Delta^{n-1} u(t), \lambda)$, along $u(t)$ and satisfies $\Delta^{i-1} w(t_0) = 0, 1 \leq i \leq n-1$, and $w(t_1) - \sum_{j=1}^m a_j w(\tau_j) = 0$. (Received August 08, 2014)