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Carlos Alberto Cadavid* (ccadavid@eafit.edu.co), **Juan Diego Velez** (jdvelez@unal.edu.co) and **Jean Carlos Cortissoz** (jean.cortissoz@gmail.com). *Minimal Morse functions via the heat equation*. Preliminary report.

Let (M, g) be a closed Riemannian manifold that is homogeneous, in the sense that each pair of points have mutually isometric neighborhoods, and let Δ_g be its Laplace-Beltrami operator. The heat equation on (M, g) is $\frac{\partial f}{\partial t} = -\Delta_g(f)$ and for each initial condition u in $L^2(M)$ there exists a unique solution $f_t(\cdot) := f(\cdot, t)$ satisfying $f_0 = u$.

It has been observed in several examples that for generic u and large enough t , that f_t is a Morse function having the least number of critical points admitted by any Morse function on M . There are examples in which this phenomenon does not hold in the form just stated, but seems to take place if one perturbs the metric g a bit. In order to probe the validity of the statement in this latter form, computational experiments have been performed in which the Riemannian manifold and its Laplace-Beltrami operator have been approximated by a graph and its Laplacian operator.

This suggests that it is worth asking whether a similar phenomenon holds for graphs. (Received August 20, 2014)