

1106-VN-1021

**John Villalpando\*** (jvillalp@callutheran.edu), California Lutheran University, 60 West Olsen Road, Thousand Oaks, CA 91360, and **Vesta Coufal, Kathie Yerion** and **Rob Ray**. *The Existence of Trees for Given Values of  $\lambda$ ,  $\bar{\kappa}$ , and  $\kappa$  for  $L(2,1)$ -Colorings and Irreducible  $L(2,1)$ -Colorings.*

An  $L(2,1)$ -coloring of a graph is a labeling of the vertices using non negative integers such that adjacent vertices differ in label by at least 2 and distance two vertices differ in label. A well studied invariant of  $L(2,1)$ -colorings, the span denoted by  $\lambda$ , is the smallest integer  $k$  for a given graph such that there exists an  $L(2,1)$ -coloring of the graph using only integers less than or equal to  $k$ . The invariant  $\bar{\kappa}$  is the least number of color classes required to create an  $L(2,1)$ -coloring on a given graph. An  $L(2,1)$ -coloring of a graph is irreducible if reducing the label on any vertex violates an  $L(2,1)$ -coloring condition. The invariant  $\kappa$  is the least number of color classes required to create an irreducible  $L(2,1)$ -coloring on a given graph. For any tree  $T$  it is known that  $\Delta + 1 \leq \bar{\kappa} \leq \kappa \leq \lambda + 1$  and  $\lambda \in \{\Delta + 1, \Delta + 2\}$  where  $\Delta$  is the maximum degree of the tree. We study the 18 possible cases of the values  $\bar{\kappa}$ ,  $\kappa$ , and  $\lambda$  on trees providing examples, families of examples or when necessary proving no such tree exists. (Received September 09, 2014)