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University Blvd., Laredo, TX 78041. *Amalgamating many Boolean algebras.*

Δ -systems of overlapping Boolean algebras always extend to a common Boolean algebra, but non- Δ -systems may not: we might have $x <_A y <_B z <_C x$. Non- Δ -systems are unavoidable when constructing a Boolean algebra (or any structure) of size $\geq \aleph_3$ as a directed union of countable structures. We prove a nontrivial sufficient condition for n overlapping Boolean algebras to have a common extension. Along the way, we prove an n -ary version of the Interpolation Theorem of propositional logic.

Using also the set-theoretic technique of long ω_1 -approximation sequences (also known as Davies sequences), we obtain a flexible method of constructing (in ZFC) arbitrarily large Boolean algebras as direct limits of countable Boolean algebras. Our main application is a Boolean algebra of size \aleph_n with the n -ary FN but not the $(n + 1)$ -ary FN where the n -ary FN is a higher-arity variant of the Freese-Nation property.

Our techniques also yield a new characterization of projective Boolean algebras that implies purely finitary facts about Vietoris hyperspace and symmetric power functors in the category of finite discrete spaces. (Received September 16, 2016)