

1125-05-1809

**Martin Rolek\*** (mrolek@knights.ucf.edu) and **Zi-Xia Song**. *Coloring graphs with forbidden minors.*

Hadwiger's conjecture from 1943 states that for every integer  $t \geq 1$ , every graph either can be  $t$ -colored or has a subgraph that can be contracted to the complete graph on  $t + 1$  vertices. Proving that graphs with no  $K_7$  minor are 6-colorable is the first case of Hadwiger's conjecture that is still open. It is not known yet whether graphs with no  $K_7$  minor are 7-colorable. Using a Kempe-chain argument along with the fact that an induced path on three vertices is dominating in a graph with independence number two, we first give a very short and computer-free proof of a recent result of Albar and Gonçalves and generalize it to the next step by showing that every graph with no  $K_t$  minor is  $(2t - 6)$ -colorable, where  $t \in \{7, 8, 9\}$ . We then prove that graphs with no  $K_8^-$  minor are 9-colorable and graphs with no  $K_8^-$  minor are 8-colorable. Finally we prove that if Mader's bound for the extremal function for  $K_p$  minors is true for all  $p \geq 10$ , then every graph with no  $K_p$  minor is  $(2t - 6)$ -colorable. We believe that the Kempe-chain method we have developed in this paper is of independent interest. (Received September 19, 2016)