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(xiaoya.zha@mtsu.edu). *Toughness condition for  $k$ -trees in  $K_4$ -minor-free graphs.*

Let  $k$  be a positive integer. A  $k$ -tree is a tree with maximum degree at most  $k$ , and a  $k$ -walk is a closed walk with each vertex repeated at most  $k$  times. A  $k$ -walk can be obtained from a  $k$ -tree by visiting each edge twice. Jackson and Wormald in 1990 conjectured that any  $\frac{1}{k-1}$ -tough graph contains a spanning  $k$ -walk for  $k \geq 2$ . This conjecture is widely open even for planar graphs. We confirm this conjecture for  $K_4$ -minor-free graphs, an important subclass of planar graphs, by showing that any  $\frac{1}{k-1}$ -tough  $K_4$ -minor-free graph contains a spanning  $k$ -tree for any integer  $k \geq 2$ . (Received September 19, 2016)