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**Rachel Kirsch\*** (rkirsch2@math.unl.edu) and **Jamie Radcliffe**. *The Maximum Number of Triangles in a Graph with a Fixed Number of Edges and Maximum Degree*. Preliminary report.

Extremal problems concerning the number of independent sets or complete subgraphs have been well studied in recent years. Cutler and Radcliffe proved that among graphs with  $n$  vertices and maximum degree at most  $r$ , where  $n = a(r+1)+b$  with  $0 \leq b \leq r$ ,  $aK_{r+1} \cup K_b$  has the maximum number of complete subgraphs, answering a question of Galvin. Gan, Loh, and Sudakov conjectured that  $aK_{r+1} \cup K_b$  also maximizes the number of complete subgraphs  $K_t$  for each fixed size  $t \geq 3$ , and proved this for  $a = 1$ . Cutler and Radcliffe proved this conjecture for  $r \leq 6$ . We investigate a variant of this problem where we fix the number of edges instead of the number of vertices. We conjecture that  $aK_{r+1} \cup C(b)$ , where  $C(b)$  is the colex graph on  $b$  edges, maximizes the number of triangles among graphs with  $m$  edges and maximum degree  $r$ , where  $m = a\binom{r+1}{2} + b$ ,  $0 \leq b < \binom{r+1}{2}$ . We prove this conjecture for  $r \leq 6$ . (Received August 14, 2016)