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Nathan Kaplan* (nkaplan@math.uci.edu), **Gautam Chinta** (gchinta@ccny.cuny.edu) and **Shaked Koplewitz** (shaked.koplewitz@yale.edu). *Counting lattices by cotype.*

The short integer solution (SIS) problem asks, given m uniformly random elements g_1, \dots, g_m from $(\mathbb{Z}/q\mathbb{Z})^n$ to find an integer vector (x_1, \dots, x_m) of small norm such that $x_1g_1 + \dots + x_mg_m = 0$. This problem plays an important role in the theory of worst-case to average-case reductions for lattice problems developed by Ajtai. This naturally leads to finding short vectors in sublattices L of \mathbb{Z}^m with $\mathbb{Z}^m/L = (\mathbb{Z}/q\mathbb{Z})^n$. In the generalized version of this problem we replace $(\mathbb{Z}/q\mathbb{Z})^n$ with a more general finite abelian group G .

The cotype of an n -dimensional lattice L is the finite abelian group \mathbb{Z}^n/L . What properties do we expect for the cotype of a randomly chosen sublattice of \mathbb{Z}^n ? How many sublattices have cotype G ? We discuss these and other problems and explain a connection to the Cohen-Lenstra heuristics from number theory. (Received September 20, 2016)