

1125-14-2021

**Martin Helmer\*** ([martin.helmer@berkeley.edu](mailto:martin.helmer@berkeley.edu)), 966 Evans Hall, Berkeley, CA 94720-3840,  
and **Jose Israel Rodriguez** and **Serkan Hosten**. *Topological Invariants and the Maximum Likelihood Degree of a Toric Variety*. Preliminary report.

Let  $X_A$  be the projective toric variety defined by an integer  $d \times n$  matrix  $A$  of rank  $d$  and let  $c$  be a general element of the associated dimension  $n$  complex algebraic torus. We show that the maximum likelihood (ML) degree of the variety  $c \cdot X_A$  obtained by the torus action of  $c$  on  $X_A$  can be seen as a coefficient of a particular component of the Chern-Mather class of  $X_A$ . This realization allows us to determine a, so called, ML discriminant for  $c \cdot X_A$ . In particular we show that if the principal A-determinant,  $E_A$ , of  $X_A$  does not vanish at  $c$  we have that  $\text{MLdegree}(c \cdot X_A)$  is given by the normalized volume of the polytope obtained by taking the convex hull of the matrix  $A$ . Using this we also confirm a known relation between the ML degree of  $c \cdot X_A$  and the Euler characteristic of an associated very affine variety. (Received September 19, 2016)