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**Iva Halacheva\*** ([i.halacheva@lancaster.ac.uk](mailto:i.halacheva@lancaster.ac.uk)), **Joel Kamnitzer**, **Leonid Rybnikov** and **Alex Weekes**. *A monodromy action on crystals and the cactus group*. Preliminary report.

The shift of argument algebras associated to a finite-dimensional reductive Lie algebra  $\mathfrak{g}$  are certain maximal commutative subalgebras of  $U(\mathfrak{g})$ . They are parametrized by a moduli space  $M_{\mathfrak{g}}$ , which in type  $A$  coincides with the Deligne-Knudson-Mumford moduli space of stable real curves of genus 0 with  $n+1$  marked points. Furthermore, they have simple spectrum when acting on an irreducible highest-weight representation, and so produce a covering of  $M_{\mathfrak{g}}$ . We show that the resulting monodromy action coincides with a combinatorial action of the cactus group on  $\mathfrak{g}$ -crystals, realized via Schützenberger involutions. (Received September 19, 2016)