

1125-34-1924

**Paul Eloe\***, 300 College Park, Dayton, OH 454692316, and **Tyler Masthay**, 300 College Park, Dayton, OH 454692316. *Uniqueness implies existence of solutions for two-point boundary value problems for fractional differential equations.*

Let  $a < b$  and assume  $1 < \alpha \leq 2$ . For each  $a < x_1 < x_2 < b$ ,  $y_1, y_2 \in \mathbb{R}$ , we consider the two-point conjugate type boundary value problem for the fractional differential equation

$$D_{*x_1}^\alpha y(x) = f(x, y(x), y'(x)), \quad x_1 < x < b, \quad (1)$$

$$y(x_1) = y_1, \quad y(x_2) = y_2, \quad (2)$$

where  $D_{*x_1}^\alpha y(x)$  denotes the Caputo fractional derivative of order  $\alpha$ . We obtain the following analogue of a well-known result for ordinary differential equations: if

**(A)**  $f : (a, b) \times \mathbb{R}^2 \rightarrow \mathbb{R}$  is continuous,

**(B)** if for each  $a < x_1 < b$ ,  $y_1, m \in \mathbb{R}$ , solutions of (1) satisfying initial conditions

$$y(x_1) = y_1, \quad y'(x_1) = m,$$

are unique and extend to all of  $(x_1, b)$ , and

**(C)** if for all  $a < x_1 < x_2 < b$ ,  $y_1, y_2 \in \mathbb{R}$ , solutions of (1), (2) are unique, when they exist,

then for all  $a < x_1 < x_2 < b$ ,  $y_1, y_2 \in \mathbb{R}$ , solutions of (1), (2) exist. (Received September 19, 2016)