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Scott A. Atkinson* (scott.a.atkinson@vanderbilt.edu). *Minimal faces and Schur's Lemma for embeddings into $R^\mathcal{U}$.*

As shown by N. Brown in 2011, for a separable II_1 -factor N , the invariant $\mathbf{Hom}(N, R^\mathcal{U})$ given by unitary equivalence classes of embeddings of N into $R^\mathcal{U}$ —an ultrapower of the separable hyperfinite II_1 -factor—takes on a convex structure. This provides a link between convex geometric notions and operator algebraic concepts; for instance, extreme points are precisely the embeddings with factorial relative commutant. The geometric nature of this invariant provides a familiar context in which natural curiosities become interesting new questions about the underlying operator algebras. For example, consider the following simple question. Can four extreme points have a planar convex hull?

In this talk we will generalize the characterization of extreme points by showing that given an embedding $\pi : N \rightarrow R^\mathcal{U}$, the dimension of the minimal face containing the equivalence class $[\pi]$ is one less than the dimension of the center of the relative commutant of π . At the same time, we will establish the “convex independence” of extreme points—providing a negative answer to the above question. Along the way we make use of a version of Schur's Lemma for this context. (Received September 19, 2016)