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A famous theorem of Mackey characterizes those unitary G -modules V that are induced from a closed subgroup $H \subset G$ by the presence of a *system of imprimitivity* based on G/H : that is, a G -invariant, commutative C^* -subalgebra of $\text{End}(V)$ whose spectrum is, as a G -space, homogeneous and isomorphic to G/H . In this work, we similarly characterize those hamiltonian G -spaces X that are induced from H (in the sense of Kazhdan-Kostant-Sternberg, 1978) by the presence of a (symplectic) *system of imprimitivity* based on G/H : that is, a G -invariant, Poisson commutative subalgebra \mathfrak{f} of $C^\infty(X)$, consisting of functions whose hamiltonian flow is complete, and such that the image of the moment map $X \rightarrow \mathfrak{f}^*$ is homogeneous and isomorphic to G/H . Likewise, we characterize induced Kostant-Souriau bundles over hamiltonian G -spaces by the presence of a (contact) system of imprimitivity. This result is a key ingredient in the Mackey ‘normal subgroup analysis’ of hamiltonian and Kostant-Souriau G -spaces. (Received September 20, 2016)