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*Computing Hypergeometric Solutions of Second Order Linear Differential Equations using
Quotients of Formal Solutions and Integral Bases.*

We present an algorithm for computing hypergeometric solutions of a second order linear differential operator L with rational function coefficients. Our algorithm searches for solutions of the form

$$\exp\left(\int r dx\right) \cdot (r_0 \cdot {}_2F_1(a_1, a_2; b_1; f) + r_1 \cdot {}_2F_1'(a_1, a_2; b_1; f))$$

where $r, r_1, r_2, f \in \overline{\mathbb{Q}(x)}$, and $a_1, a_2, b_1 \in \mathbb{Q}$. Our algorithm has two components. The first tries to simplify L using normalized integral bases. The goal is to reduce r_1 to 0. The second component tries to find a_1, a_2, b_1, f using quotients of formal solutions, modular reduction, Hensel lifting, and rational reconstruction. (Received September 15, 2016)