

1125-VN-2044      **Nicholas Heiner** (heiner@hendrix.edu) and **Duff Campbell\*** (campbell@hendrix.edu).

*Generalizing the convergent to a simple continued fraction.*

If we write the simple continued fraction  $a_0 + \frac{1}{a_1 + \frac{1}{a_2 + \dots}}$  as  $[a_0; a_1, a_2, \dots]$ , then the convergents are well-known as  $\frac{h_n}{k_n}$ , where  $h_n = a_n h_{n-1} + h_{n-2}$  and  $k_n = a_n k_{n-1} + k_{n-2}$  for  $n \geq 0$ ; the four numbers  $h_{-1} = 1, h_{-2} = 0, k_{-1} = 0, k_{-2} = 1$  set “initial conditions” so that the first two convergents are, appropriately,  $\frac{h_0}{k_0} = a_0$  and  $\frac{h_1}{k_1} = \frac{a_0 a_1 + 1}{a_1} = a_0 + \frac{1}{a_1}$ . Nicholas Heiner made it his senior project to generalize these initial conditions, and thus  $h_{-1} = b, h_{-2} = a, k_{-1} = d, k_{-2} = c$  are arbitrary. Several interesting theorems were discovered, as well as other conjectures which remain as yet unproven. (Received September 19, 2016)