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**Rose McCarty\*** (rmccarty3@gatech.edu), **Becky Eastham**, **Paul Han**, **Bill Kay** and **David Spencer**. *Total Acquisition in Diameter 2 Graphs and Tournaments*. Preliminary report.

Let  $G$  be a graph where each vertex is given an initial weight of 1. At each time step, a vertex  $u$  may **acquire** all of the weight from a vertex  $v \in N(u)$  if  $w(u) \geq w(v)$ . After this acquisition move, the new weight on  $u$  is  $w(u) + w(v)$  and the new weight on  $v$  is 0. The total acquisition number of a graph  $a_t(G)$  is the smallest integer so that there exists a sequence of acquisition moves ending with  $a_t(G)$  vertices having weight greater than 0. LeSaulnier, Prince, Wenger, West, and Worah prove that, for  $G$  a diameter 2 graph with no 4-cycles,  $a_t(G) \leq 2$ . They further show that if  $G$  has diameter 2, then  $a_t(G) \leq 32 \ln n \ln \ln n$ , and conjecture that in fact, the total acquisition number of any diameter 2 graph is less than 2. We show that when  $G$  is a diameter 2 graph where every 4-cycle in  $G$  induces a  $K_4$ ,  $a_t(G) \leq 2$ . We also give an additional family of diameter 2 graphs with acquisition number less than or equal to 2. Finally, we prove that all tournaments have acquisition number less than or equal to 2 for a suitable variant of acquisition on directed graphs. (Received September 22, 2015)