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The Heisenberg group  $\mathbb{H}$  is an important example in analysis (e.g. several complex variables), geometry (e.g. complex hyperbolic), algebra (e.g. nilpotent groups), and applications (e.g. math biology). It is therefore imperative that, given a metric space  $X$ , we are able to say when it is essentially the same as  $\mathbb{H}$  in that there exists a bi-Lipschitz mapping  $f : X \rightarrow \mathbb{H}$ .

I exhibit a family of metric doubling measures on  $\mathbb{H}$ , weighting Lebesgue measure with (the exponential of) certain logarithmic potentials. Each associated metric is shown to be bi-Lipschitz equivalent to the usual sub-Riemannian metric on  $\mathbb{H}$  by constructing a quasiconformal mapping of  $\mathbb{H}$  with Jacobian comparable to the weighting. To do this I establish results of independent interest in the theory of quasiconformal flows on  $\mathbb{H}$ , building on the work of Korányi and Reimann. The scheme follows analogous work of Bonk, Heinonen and Saksman in the Euclidean setting.

Along the way I confront the limitations of conformal mappings of  $\mathbb{H}$ , explain how the radial stretch mappings of Balogh, Fässler and Platis inspired a key step, and mention future work on a possible connection to the CR notion of  $Q$ -curvature. (Received September 20, 2015)