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**Michał Adamaszek, Henry Adams\*** (adams@math.colostate.edu) and **Samadwara Reddy**.  
*Vietoris–Rips complexes of circles and ellipses.*

Given a metric space  $X$  and a distance threshold  $r > 0$ , the Vietoris–Rips simplicial complex has as its simplices the finite subsets of  $X$  of diameter less than  $r$ . If  $X$  is a Riemannian manifold and  $r$  is sufficiently small then the Vietoris–Rips complex is homotopy equivalent to the original manifold, but little is known about Vietoris–Rips complexes for larger values of  $r$  even though they are used in applications of persistent homology. We show that as  $r$  increases, the Vietoris–Rips complex of the circle obtains the homotopy types of the circle, the 3-sphere, the 5-sphere, the 7-sphere,  $\dots$ , until finally it is contractible. Paradoxically, we show that the Vietoris–Rips complex of an arbitrarily dense subset of the ellipse need not be homotopy equivalent to the Vietoris–Rips complex of the entire ellipse. (Received September 14, 2015)