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**Joungmin Song\*** (songj@gist.ac.kr), Gwangju Institute of Science and Technology, Cheomdan Gwagiro 123, GIST College Bldg A-410, Gwangju, 61005, South Korea. *Characteristic polynomial of hyperplane arrangements via enumerative combinatorics and finite field method.*

A hyperplane arrangement is a finite set of affine hyperplanes in a real affine space. Let  $\mathcal{J}_n$  be the hyperplane arrangement consisting of all hyperplanes (or walls)  $H_{ij}$ ,  $0_k$ ,  $1_l$ , where, for each  $i, j, k$ , and  $l \in \{1, 2, \dots, n\}$ ,

$$H_{ij} := \{\mathbf{x} \in \mathbb{R}^n \mid x_i + x_j = 1\} = H_{ji}$$

and

$$0_k := \{\mathbf{x} \in \mathbb{R}^n \mid x_k = 0\}, \text{ and } 1_l := \{\mathbf{x} \in \mathbb{R}^n \mid x_l = 1\}.$$

The number of the *regions*, i.e., the connected components of  $\mathbb{R}^n \setminus \bigcup_{H \in \mathcal{J}_n} H$  is given by the characteristic polynomial  $\chi_n(t)$ . We formulate  $\chi_n(t)$  via enumerative combinatorics and finite field method. We give a direction forward generalizing this process to  $\mathcal{H}_n$ , whose walls are of the form

$$w_S = \left\{ \mathbf{x} \in \mathbb{R}^n \mid \sum_{i \in S} x_i = 1 \right\}.$$

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