Given an edge-labeled graph, a generalized spline is a way of labeling the vertices so that each pair of adjacent vertex-labels differs by a multiple of the label on the edge between them. When edges are labeled by polynomials, this definition is a natural extension of the definition of splines from applied mathematics and analysis. We describe several new results on generalized splines, including connections to geometry. (Received September 26, 2017)