

1135-05-2907

**Sam Bardwell-Evans\*** (sbardwel@caltech.edu). *A Generalization of the Carlson-Simpson Theorem Analogous to Gowers' Theorem*. Preliminary report.

We prove a generalization of Carlson and Simpson's Dual Ramsey Theorem that is analogous to Gowers' theorem for  $\text{FIN}_k$ . Instead of considering the tetris operation  $T : \{0, \dots, k\} \rightarrow \{0, \dots, k-1\}$ , we fix a finite, non-empty alphabet  $A$  and consider analogous functions  $f : A \cup \{0, \dots, k\} \rightarrow A \cup \{0, \dots, k-1\}$ , and instead of finding an infinite sequence of functions  $b_n$  in  $\text{FIN}_k$  such that the set of all finite sums  $\sum T^{d_n}(b_n)$  is monochromatic, we find an infinite sequence of (not necessarily finitely supported) functions  $b_n : \omega \rightarrow A \cup \{0, \dots, k-1\}$  such that the set of all (not necessarily finite) sums  $\sum f_n(b_n)$  is monochromatic. The natural multidimensional generalization of this theorem implies the Carlson-Simpson Theorem. (Received September 26, 2017)