

1135-05-2955

Huseyin Acan*, huseyin.acan@rutgers.edu, and **Jeff Kahn**. *Disproof of a conjecture of Alon and Spencer.*

Let ν_k denote the size of a largest family of edge-disjoint k -cliques that can be packed into the random graph $G = G_{n,1/2}$. Alon and Spencer conjectured the expected value of ν_k to be $\Omega(n^2/k^2)$ when k is slightly smaller than the clique number of G . We disprove this conjecture by showing that the expected value in question is $O(n^2/k^3)$.

Our main interest lies in answering the following more general question. Let $k \ll \sqrt{n}$ and A_1, \dots, A_t be random k -subsets of $[n]$, chosen uniformly and independently. Then what can we say about the probability

$$\mathbb{P}(|A_i \cap A_j| \leq 1 \forall i \neq j)?$$

We provide upper bounds for this probability that almost agree with the values obtained by pretending the events $\{|A_i \cap A_j|\}_{i < j}$ are independent. (Received September 26, 2017)