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**Ashvin Anand Swaminathan\*** (ashvins@math.princeton.edu), 1 Lawrence Drive, Apartment #808, Princeton, NJ 08540, and **Anand Patel** (anand.patel@okstate.edu). *Inflectionary Invariants for Plane Curve Singularities.*

Let  $k$  be an algebraically closed field of characteristic 0, and let  $f \in k[[x, y]]$  be the germ of an isolated plane curve singularity. We study the role of the singularity germ  $f$  in the analysis of inflectionary behavior of curves specializing to a curve with a singularity cut out by  $f$ . We introduce a numerical function  $m \mapsto \text{AD}^m(f)$ , an invariant canonically associated to the isomorphism class of the singularity germ  $f$ , which arises as an error term in the problem of enumerating  $m^{\text{th}}$ -order inflection points in a 1-parameter family of curves acquiring a singular member with singularity given by  $f = 0$ . For an ordinary nodal singularity  $f = xy$ , we explicitly compute  $\text{AD}^m(f) = \binom{m+1}{4}$ , and we deduce as a corollary that  $\text{AD}^m(f) \geq \mu_f \cdot \binom{m+1}{4}$  for an arbitrary  $f$ , where  $\mu_f$  is the Milnor number of  $f$ . The numerical function  $m \mapsto \text{AD}^m(f) - \mu_f \cdot \binom{m+1}{4}$  is thus also an invariant of the singularity type, and it measures the extent to which the singularity counts as an  $m^{\text{th}}$ -order inflection point. Our main results can be applied to address a broad range of enumerative questions concerning inflection points in families of curves. (Received September 16, 2017)