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**Dallas Smith\*** (dallas.smith@mathematics.byu.edu), Provo, UT 84606, and **Ben Webb** (bwebb@mathematics.byu.edu), **Amanda Francis** (afrancis@carroll.edu) and **Derek Sorensen** (derek.sorensen@maths.ox.ac.uk). *Applications of Equitable Decompositions for Graphs with Symmetries.*

The symmetries of a graph are characterized by the graph's set of automorphisms. If a graph  $G$  has a symmetry, it is possible to decompose any automorphism compatible matrix  $M$  associated with  $G$ , such as its adjacency and Laplace matrices, into a number of smaller matrices  $M_1, \dots, M_n$ . These smaller matrices collectively have the same eigenvalues as the original matrix  $M$  including multiplicities. This process is referred to as an equitable decomposition. Here we discuss a number of applications of this decomposition. First we demonstrate that not only can a matrix  $M$  be decomposed but that the eigenvectors of  $M$  can also be equitably decomposed. Additionally, we prove under mild conditions that if a matrix  $M$  is equitably decomposed the resulting divisor matrix, which is the divisor matrix of the associated equitable partition, will have the same spectral radius as the original matrix  $M$ . Finally, we describe how an equitable decomposition effects the Gershgorin region of a matrix  $M$ , which can be used to localize the eigenvalues of  $M$ . (Received September 25, 2017)