We study the asymptotic integration problem for higher order nonlinear delay differential equations of the form $L_n x(t) = f(t, x(g(t)))$, where $L_n$ is a linear operator. It is shown that solutions are asymptotic to prescribed solutions of $L_n x = 0$ at infinity. (Received September 26, 2017)