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Kathryn McCormick* (kathryn-mccormick@uiowa.edu), University of Iowa, 14 MacLean Hall, Iowa City, IA 52246. *Holomorphic Bundles Over Riemann Surfaces and Subalgebras of n -homogeneous C^* -algebras.*

Let \bar{R} denote a finite bordered Riemann surface, and let $\Gamma_c(\bar{R}, \mathfrak{E}(\bar{R}))$ denote the continuous sections of a flat, matrix $PU_n(\mathbb{C})$ -bundle over \bar{R} , $\mathfrak{E}(\bar{R})$. We write $\Gamma_h(\bar{R}, \mathfrak{E}(\bar{R}))$ for the collection of continuous sections of $\mathfrak{E}(\bar{R})$ that are holomorphic on the interior of \bar{R} . This is a subalgebra of the C^* -algebra of continuous sections, $\Gamma_c(\bar{R}, \mathfrak{E}(\bar{R}))$. Our first goal is to calculate the boundary representations of $\Gamma_c(\bar{R}, \mathfrak{E}(\bar{R}))$ for $\Gamma_h(\bar{R}, \mathfrak{E}(\bar{R}))$, in the sense of Arveson, showing that they are point evaluations on the boundary of \bar{R} . Our second goal is to show $\Gamma_h(\bar{R}, \mathfrak{E}(\bar{R}))$ is an Azumaya algebra over its center. Together, these two theorems indicate a sense in which our algebra $\Gamma_h(\bar{R}, \mathfrak{E}(\bar{R}))$ is a nonselfadjoint generalization of an n -homogeneous C^* -algebra. (Received September 23, 2017)