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Gerald Beer and **Colin Bloomfield*** (colinbloomfield1@gmail.com), 405 Lewis st., Los Angeles, CA 90042. *A Closure Operator for Clopen Topologies.*

A topology τ on a nonempty set X is called a clopen topology provided each member of τ is both open and closed. Given a function f from X to Y , the operator $E \mapsto f^{-1}(f(E))$ is a closure operator on the power set of X whose fixed points are closed subsets corresponding to a clopen topology on X . Conversely, for each clopen topology τ on X , we produce a function f with domain X such that $\tau = \{E \subseteq X : E = f^{-1}(f(E))\}$. We characterize the clopen topologies on X as those that are weak topologies determined by a surjective function with values in some discrete topological space. Paralleling this result, we show that a topology admits a clopen base if and only if it is a weak topology determined by a family of functions with values in discrete spaces. (Received September 19, 2017)