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**Fortunata Aurora Basile\*** (basilef@unime.it), **Maddalena Bonanzinga** and **Nathan Carlson**. *New cardinality bounds for Urysohn spaces.*

Sapirskii proved that  $|X| \leq \pi\chi(X)^{c(X)\psi(X)}$ , for a regular space  $X$ . We introduce the  $\theta$ -pseudocharacter of a Urysohn space  $X$ , denoted by  $\psi_\theta(X)$ , and prove that if  $X$  is a Urysohn space then  $|X| \leq \pi_\chi(X)^{Uc(X)\psi_\theta(X)}$ . The Urysohn cellularity of a space  $X$ , defined by Schröder, satisfies  $Uc(X) \leq c(X)$  and  $\psi(X) \leq \psi_c(X) \leq \psi_\theta(X) \leq \chi(X)$ . Note that if  $X$  is a regular space then  $Uc(X) = c(X)$  and  $\psi(X) = \psi_\theta(X)$ .

We also introduce new cardinal invariants:  $\theta$ - $aL(X)$ ,  $\theta$ - $aL'(X)$  and  $t_{\hat{c}}(X)$  in order to prove that if  $X$  is a Urysohn space then  $|X| \leq 2^{\theta-aL'(X)t_{\hat{c}}(X)\psi_\theta(X)}$  (\*). As  $\theta$ - $aL(X) \leq aL(X)$  and  $t_{\hat{c}}(X)\psi_\theta(X) \leq \chi(X)$ , this represents an improvement of the Bella-Cammaroto inequality  $|X| \leq 2^{aL(X)\chi(X)}$ . The invariant  $\theta$ - $aL'(X)$  is constructed by using maximal filters on the family of finite intersections of regular closed sets. Finally, we introduce a new class of topological spaces called *weakly H-closed*, a property related to H-closedness. It follows from (\*) that if  $X$  is a Urysohn, weakly H-closed space then  $|X| \leq 2^{\chi(X)}$ . (Received September 23, 2017)