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Greg Malen* (gmalen@math.duke.edu). *Dense Random Clique Complexes.*

One model for percolation on high-dimensional simplicial complexes is $X(n, p)$, the probably space of Vietoris–Rips complexes, or clique complexes, on n vertices where each edge appears independently with probability p . This is a natural extension of the Erdős–Rényi random graph model $G(n, p)$ into higher dimensions. Whereas the random d -dimensional complexes $Y_d(n, p)$ provide high-dimensional analogues to the phase transitions observed in sparse Erdős–Rényi random graphs, here we examine the evolution of $X(n, p)$ as p increases into the dense and super-dense regimes. In particular, around middle dimension we exhibit non-trivial homology in an interval with length that increases from arbitrary finite lengths when $p = (\log n)^{-\alpha}$, to $O(\log \log n)$ when p is constant. We also discuss various homology vanishing and collapsibility results, and examine bounds for the threshold in p at which $X(n, p)$ becomes contractible with high probability. (Received September 25, 2017)