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In 1976, Chapman-Siebenmann provided criteria for a Hilbert cube manifold X to admit a \mathcal{Z} -compactification. However, the question of (whether) the extension of their characterization can be extended to manifolds still remains open: If M^n is a finite dimensional manifold and $M^n \times \mathcal{Q}$ is \mathcal{Z} -compactifiable, is M^n itself \mathcal{Z} -compactifiable? In this talk, the complete characterizations of completable manifolds and pseudo-collarable manifolds will be given, respectively. As two applications, the former one implies a best possible "stabilization theorem": $M^n \times \mathcal{Q}$ ($n \geq 4$) is \mathcal{Z} -compactifiable iff $M^n \times [0, 1]$ is \mathcal{Z} -compactifiable. Applying the latter characterization together with knot theory and group theory, we prove that there exist \mathcal{Z} -compactifiable manifolds with boundary which are not pseudo-collarable. This can be viewed as a counterexample of a special case of a question asked by Guilbault-Tinsley [2003]: Can a \mathcal{Z} -compactifiable open manifold fail to be pseudo-collarable? (Received September 23, 2017)