In this talk we discuss how an elementary course in cryptography can be used as a gateway to expose students to core mathematical ideas such as group theory, number theory, and linear algebra, among others. (Received August 18, 2017)