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**Pallavi Mishra\***, Department of Mathematics, IIT Kharagpur, Kharagpur, India, and  
**Dharmendra Kumar Gupta**, Department of Mathematics, Indian Institute of Technology,  
Kharagpur, Kharagpur, India. *A graph-based approach for counting all Sudoku squares of rank  $n$ .*

This paper deals with a graph-based approach for counting all Sudoku squares of rank  $n$ . First, all the S-permutations are generated and an S-permutation graph  $G_s = (V_s, E_s)$  is constructed in which vertices represent S-permutations and two vertices are connected by an edge if and only if their corresponding S-permutations are not disjoint to each other. A set of mutually disjoint S-permutations corresponds to an independent set of  $G_s$ . A vertex  $v \in V_s$  is selected randomly and an induced subgraph  $\hat{G}_s = (\hat{V}_s, \hat{E}_s)$  of  $G_s$  is derived by considering all mutually disjoint vertices to  $v$ . There is a one to one correspondence between a maximum independent set of  $\hat{G}_s$  together with  $v$  and a Sudoku square. Now, an algorithm is developed to count all the maximum independent sets of  $\hat{G}_s$  which are equal to all Sudoku squares of rank  $n$ . The correctness of the algorithm is shown and its time complexity is  $O(3^{\frac{\xi_n}{3}})$ , where  $\xi_n$  is the total number of S-permutations mutually disjoint to an S-permutation. The algorithm is experimentally tested for Sudoku squares of rank up to 3. An upper bound on the total number of Sudoku squares is also derived. (Received September 23, 2017)