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On a Waring's problem for integral quadratic and hermitian forms.

For each positive integer n , let $g_{\mathbb{Z}}(n)$ be the smallest integer such that if an integral quadratic form in n variables can be written as a sum of squares of integral linear forms, then it can be written as a sum of $g_{\mathbb{Z}}(n)$ squares of integral linear forms. We show that as n goes to infinity, the growth of $g_{\mathbb{Z}}(n)$ is at most an exponential of \sqrt{n} . Our result improves the best known upper bound on $g_{\mathbb{Z}}(n)$ which is in the order of an exponential of n . We also define an analogous number $g_{\mathcal{O}}^*(n)$ for writing hermitian forms over the ring of integers \mathcal{O} of an imaginary quadratic field as sums of norms of integral linear forms, and when the class number of the imaginary quadratic field is 1, we show that the growth of $g_{\mathcal{O}}^*(n)$ is at most an exponential of \sqrt{n} . (Received September 23, 2017)