In this talk, we will illustrate two explicit methods which lead to special $L$-values of certain modular forms admitting complex multiplication, motivated in part by properties of $L$-functions obtained from Calabi-Yau manifolds defined over $\mathbb{Q}$. (Received September 23, 2018)