The notion of a braided module category over a braided monoidal category comes naturally from the study of extensions of braided categories. The 2-category of braided module categories comes equipped with interesting structures. This is a report on the joint work with D. Nikshych. (Received September 25, 2018)