Gravitational lensing provides a beautiful connection between astrophysics and mathematics. I will show examples of connections that involve catastrophe theory, complex analysis, the Poincare-Hopf index theorem, and stochastic processes. I will strive to explain how astrophysical applications both motivate and benefit from deep study of the mathematics of gravity and light. (Received September 25, 2018)