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**Jason P Bell\*** (jpbell@uwaterloo.ca), **Dragos Ghioca** and **Matthew Satriano**. *A gap conjecture for heights of iterates.*

Let  $X$  be a quasi-projective variety defined over a field  $K$  of characteristic 0, endowed with the action of an étale endomorphism  $\Phi$ , and  $f: X \rightarrow Y$  is a morphism with  $Y$  a quasi-projective variety defined over  $K$ . Then we show that a uniform result of the following type holds: if for a given  $x \in X(K)$ , for each  $y \in Y(K)$  the set  $S_y := \{n \in \mathbb{N}: f(\Phi^n(x)) = y\}$  is finite, then there exists a positive integer  $N$  such that  $\#S_y \leq N$  for each  $y \in Y(K)$ . We use this to prove that a “gap” theorem holds for étale endomorphisms, which we now describe. Let  $K$  be a number field,  $f: X \rightarrow \mathbb{P}^1$  a rational map, and  $\Phi$  be an étale endomorphism of  $X$ . If  $\mathcal{O}$  denotes the forward orbit of  $x$  under the action of  $\Phi$ , then either  $f(\mathcal{O})$  is finite, or  $\limsup_{n \rightarrow \infty} h(f(\Phi^n(x)))/\log(n) > 0$ , where  $h(\cdot)$  represents the usual logarithmic Weil height for algebraic points. We conjecture that this dichotomy should hold for general endomorphisms of quasi-projective varieties when everything is defined over a number field. (Received September 05, 2019)