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**Thomas Marley.** *Frobenius and Homological Dimensions of Complexes.*

It is proved that a module  $M$  over a Noetherian local ring  $R$  of prime characteristic and positive dimension has finite flat dimension if  $\mathrm{Tor}_i^R({}^eR, M) = 0$  for  $\dim R$  consecutive positive values of  $i$  and infinitely many  $e$ . Here  ${}^eR$  denotes the ring  $R$  viewed as an  $R$ -module via the  $e$ th iteration of the Frobenius endomorphism. In the case  $R$  is Cohen-Macualay, it suffices that the Tor vanishing above holds for a single  $e \geq \log_p e(R)$ , where  $e(R)$  is the multiplicity of the ring. This improves a result of D. Dailey, S. Iyengar, and the second author, as well as generalizing a theorem due to C. Miller from finitely generated modules to arbitrary modules. We also show that if  $R$  is a complete intersection ring then the vanishing of  $\mathrm{Tor}_i^R({}^eR, M)$  for single positive values of  $i$  and  $e$  is sufficient to imply  $M$  has finite flat dimension. This extends a result of L. Avramov and C. Miller. (Received September 11, 2019)