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**Robert L. Bryant\*** (bryant@math.duke.edu), Duke Mathematics Department, PO Box 90320, Durham, NC 27708-0320. *On solitons for the closed G<sub>2</sub>-Laplacian flow*. Preliminary report.

For G<sub>2</sub>-structures on 7-manifolds, there is a natural analog of the Ricci-flow studied in Riemannian geometry, namely, one considers a 1-parameter family  $\sigma = \sigma(t)$  of G<sub>2</sub>-structures on a given 7-manifold that satisfies the equation

$$\frac{d\sigma}{dt} = \Delta_\sigma \sigma$$

with a specified initial G<sub>2</sub>-structure  $\sigma(0) = \sigma_0$ .

When the 1-parameter family  $\sigma$  moves by diffeomorphism and scaling, we say that  $\sigma$  is a *soliton* for the G<sub>2</sub>-Laplacian flow. The most interesting case is when the initial G<sub>2</sub>-structure is *closed*.

In this talk, I will describe some of what is known about the existence and local generality of solitons for this flow, concluding with a discussion of the still-unsolved problem of the generality of the *gradient* solitons, which are of great interest in the theory of G<sub>2</sub>-structures. (Received August 26, 2019)