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**Erik Davis** and **Sunder Sethuraman\*** (sethuram@math.arizona.edu). *Approximating geodesics via random points.*

Given a ‘cost’ functional  $F$  on paths  $\gamma$  in a domain  $D \subset \mathbb{R}^d$ , in the form  $F(\gamma) = \int_0^1 f(\gamma(t), \dot{\gamma}(t)) dt$ , it is of interest to approximate its minimum cost and geodesic paths. Let  $X_1, \dots, X_n$  be points drawn independently from  $D$  according to a distribution with a density. Form a random geometric graph on the points where  $X_i$  and  $X_j$  are connected when  $0 < |X_i - X_j| < \epsilon$ , and the length scale  $\epsilon = \epsilon_n$  vanishes at a suitable rate.

For a general class of functionals  $F$ , using a form of Gamma convergence, we show that the minimum costs and geodesic paths, with respect to approximating discrete ‘cost’ functionals, built from the random geometric graph, converge almost surely in various senses to those corresponding to the continuum cost  $F$ , as the number of sample points diverges. (Received September 14, 2019)