We will discuss the general theory of cyclic $\mathbb{F}_q$-linear $\mathbb{F}_{q^t}$ codes including their count and methods to construct them. We will also construct and count these codes that are self-orthogonal or self-dual under various appropriate inner products. (Received September 03, 2019)