Mosaic knitting, a form of two-color knitting developed by designer Barbara Walker in the 1970’s, has gained popularity because it is easier for the knitter than most traditional forms of color work. The price of this ease is an unusual set of restrictions on color placement, and the core of our work is a classification of the color-swapping symmetries that are possible within these constraints. (Received September 17, 2019)