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**Karoly Bezdek\*** (kbezdek@ucalgary.ca), Dept. of Math. and Stats., University of Calgary, Calgary, Alberta T2N 1N4, Canada, and **Zsolt Langi**, Budapest University of Technology, Budapest, Hungary. *Minimizing the mean projections of finite  $\rho$ -separable packings.*

A packing of translates of a convex body in the  $d$ -dimensional Euclidean space  $\mathbb{E}^d$  is said to be totally separable if any two packing elements can be separated by a hyperplane of  $\mathbb{E}^d$  disjoint from the interior of every packing element. We call the packing  $\mathcal{P}$  of translates of a centrally symmetric convex body  $\mathbf{C}$  in  $\mathbb{E}^d$  a  $\rho$ -separable packing for given  $\rho \geq 1$  if in every ball concentric to a packing element of  $\mathcal{P}$  having radius  $\rho$  (measured in the norm generated by  $\mathbf{C}$ ) the corresponding sub-packing of  $\mathcal{P}$  is totally separable. The main result of this paper is the following theorem. Consider the convex hull  $\mathbf{Q}$  of  $n$  non-overlapping translates of an arbitrary centrally symmetric convex body  $\mathbf{C}$  forming a  $\rho$ -separable packing in  $\mathbb{E}^d$  with  $n$  being sufficiently large for given  $\rho \geq 1$ . If  $\mathbf{Q}$  has minimal mean  $i$ -dimensional projection for given  $i$  with  $1 \leq i < d$ , then the convex polytope  $\mathbf{P}$  which is the convex hull of the centres of the packing elements is approximately a  $d$ -dimensional ball. This extends a theorem of K. Böröczky Jr. (1994) from translative packings to  $\rho$ -separable translative packings for  $\rho \geq 1$ . (Received February 18, 2018)