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*Low-degree testing for quantum states.*

For any integer  $n \geq 2$  we construct a one-round two-player game  $G_n$ , with communication that scales poly-logarithmically with  $n$ , having the following properties. First, there exists an entangled strategy that wins with probability 1 and in which the players perform generalized Pauli measurements on their respective share of an  $n$ -qudit maximally entangled state, with local dimension  $q = \text{poly log}(n)$ . Second, any strategy that succeeds with probability at least  $1 - \varepsilon$  must be within distance  $O((\log n)^c \varepsilon^{1/d})$ , for universal constants  $c, d \geq 1$ , of the perfect strategy, up to local isometries. This is an exponential improvement on the size of any previously known game certifying  $\Omega(n)$  qudits of entanglement with comparable robustness guarantees. The construction of the game  $G_n$  is based on the classical test for low-degree polynomials of Raz and Safra, which we extend to the quantum regime. We further obtain several consequences for complexity theory, most notably that it is QMA-hard, under randomized reductions, to approximate up to a constant factor the maximum acceptance probability of a multiround, multiplayer entangled game with  $\text{poly log}(n)$  bits of classical communication. (Received February 14, 2018)