The main result of the present paper are following theorem.

**Theorem.** Let \( \mathcal{D} \in \mathbb{C}^{n-1} \) a bounded domain of Lyapunov and \( f'(z, z_n) \) is a holomorphic function in the cylinder \( D = \mathcal{D} \times U \) and continuous on the \( \overline{D} \). If for each fixed \( a \) in some set \( E \subset \partial \mathcal{D} \), with positive measure \( \text{mes} E > 0 \), the function \( f'(a, z_n) \) of \( z_n \) can be continued to a function holomorphic or the whole plane with the exception of some finite set(polar set) singularities then \( f'(z, z_n) \) can be holomorphically continued to \( (\mathcal{D} \times C) \setminus S \), where \( S \) is some analytic (pluripolar) subset of \( \mathcal{D} \times C \). (Received September 30, 2004)