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We study properties of (fairly) general pullback diagrams. Let  $D$  and  $T$  be domains, let  $I$  be an ideal of  $T$ , let  $\varphi : T \rightarrow T/I = E$  be the canonical map, and let  $R = \varphi^{-1}(D)$ . One of our main results describes when  $R$  is a Prüfer  $v$ -multiplication domain under a mild additional hypothesis on  $I$ . To state the result, we need a variation of the  $t$ -operation. For domains  $D \subseteq E$  and a nonzero ideal  $A$  of  $D$ , set  $A_{\tilde{v}} = (D :_E (D :_E A))$  and  $A_{\tilde{t}} = \bigcup B_{\tilde{v}}$ , where the union is taken over all finitely generated subideals  $B$  of  $A$ . The  $\tilde{v}$ - and  $\tilde{t}$ -operations have many of the properties of a star operation. We say that  $D$  is a *Prüfer  $v$ -multiplication domain with respect to  $E$*  (an  $E$ -PVMD) if each nonzero ideal  $A$  of  $D$  satisfies  $(AA^{-1})_{\tilde{t}} = D$ . Under the assumption that  $I$  is a maximal  $t$ -ideal of  $T$ , we prove that  $R$  is a PVMD if and only if  $T$  is a PVMD,  $D$  and  $E$  have the same quotient field, and  $D$  is an  $E$ -PVMD. We also give several consequences of this. (Received September 28, 2005)