

1014-39-1706

**Kenneth S. Berenhaut** (berenhks@wfu.edu), Department of Mathematics, Wake Forest University, Winston Salem, NC 27109, **John D. Foley\*** (folejd4@wfu.edu), Department of Mathematics, Wake Forest University, Winston Salem, NC 27109, and **Stevo Stević** (sstevic@ptt.yu, sstevo@matf.bg.ac.yu), Mathematical Institute of Serbian Academy of, Knez Mihailova 35/I 11000, Beograd, Serbia and Montenegro. *The Periodic Character of the Rational Difference Equation  $y_n = 1 + \frac{y_{n-k}}{y_{n-m}}$ .*

This talk explores the behavior of positive solutions of the recursive equation

$$y_n = 1 + \frac{y_{n-k}}{y_{n-m}}, \quad n = 0, 1, 2, \dots,$$

with  $y_{-s}, y_{-s+1}, \dots, y_{-1} \in (0, \infty)$  and  $k, m \in \{1, 2, 3, 4, \dots\}$ , where  $s = \max\{k, m\}$ . The main result is that if  $2^i$  is the highest power of 2 which divides  $m$ , then if  $2^{i+1} \nmid k$ ,  $y_n$  tends to 2, exponentially, and otherwise every solution tends to a period  $t$  solution, with  $t = 2 \operatorname{gcd}(k, m)$ . This generalizes several known results including that in W. T. Patula and H. D. Voulov, On the oscillation and periodic character of a third order rational difference equation. *Proc. Amer. Math. Soc.* **131** (2003), no. 3, 905–909, where the result was proven for the case  $k = 2$  and  $m = 3$ . (Received September 28, 2005)