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This talk explores the behavior of positive solutions of the recursive equation

$$y_n = 1 + \frac{y_{n-k}}{y_{n-m}}, \quad n = 0, 1, 2, \dots,$$

with $y_{-s}, y_{-s+1}, \dots, y_{-1} \in (0, \infty)$ and $k, m \in \{1, 2, 3, 4, \dots\}$, where $s = \max\{k, m\}$. The main result is that if 2^i is the highest power of 2 which divides m , then if $2^{i+1} \nmid k$, y_n tends to 2, exponentially, and otherwise every solution tends to a period t solution, with $t = 2 \gcd(k, m)$. This generalizes several known results including that in W. T. Patula and H. D. Voulov, On the oscillation and periodic character of a third order rational difference equation. *Proc. Amer. Math. Soc.* **131** (2003), no. 3, 905–909, where the result was proven for the case $k = 2$ and $m = 3$. (Received September 28, 2005)